5.1 Angles of Triangles



Geometry 5.1	Name:
Δ ABC has vertices A(0, 0), B(3, 3), and C(-3, 3). Classify it by is sides. Then determined	ermine if it is a right triangle.
Zhbe has vertices h(0, 0), b(0, 5), and e(0, 5). Classify it by is sides. Then ded	
Triangle Sum Theorem The of the of the interior angles of a triangle is	A
Exterior Angle Theorem The measure of an angle of a triangle the of the	$A \xrightarrow{1} \xrightarrow{1} \xrightarrow{C} \xrightarrow{T}$
Corollary to the Triangle Sum Theorem The of a triangle are	
Find the measure of ∠1 in the diagram.	$3x^{\circ}$ 40° 1 (5x - 10)°
Find the measures of the acute angles in the diagram.	$\frac{2x^{\circ}}{(x-6)^{\circ}}$

Assignment: 228 #2, 4, 6, 10, 12, 14, 16, 18, 20, 22, 24, 26, 28, 32, 42, 44, 48, 55, 58, 59 = 20 total

5.2 Apply Congruence and Triangles



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Geometry 5.2	Name:
Properties of Congruence of Triangles	
Congruence of triangles is,, and,	
In the diagram, what is m∠DCN? By the definition of congruence, what additional information is needed to know th	$D = \frac{N}{C} = \Delta NSR?$
Assignment: 235 #2, 3, 4, 6, 8, 10, 12, 13, 14, 15, 17, 18, 20, 21, 24, 26, 28, 30, 31, 3	32 = 20 total

5.3 Proving Triangle Congruence by SAS



Given: *B* is the midpoint of \overline{AD} . $\angle ABC$ and $\angle DBC$ are right angles. Prove: $\triangle ABC \cong \triangle DBC$

Statements	Reasons
1.	1.
2.	2.
3.	3.
4.	4.
F	
5.	5.



What can you conclude about $\triangle PTS$ and $\triangle RTQ$? Explain.



Assignment: 241 #2, 4, 6, 7, 8, 10, 12, 17, 18, 19, 23, 24, 27, 29, 31 = 15 total

5.4 Equilateral and Isosceles Triangles

Parts of an Isosceles Triangle	
	\bigwedge
Base Angles Theorem	/ \
If sides of a are, then the opposite them are	メ X
Converse of Base Angles Theorem	— <u> </u>
If angles of a are, then thesides opposite them are	
Complete the statement $I_{\text{F}} = \frac{1}{2} $	H
If $HG \cong HK$, then $\angle ___ \cong \angle __$.	
If \angle KHJ $\cong \angle$ KJH, then $\underline{\qquad} \cong \underline{\qquad} \underline{\qquad} \underline{\qquad} \underline{\qquad} \underline{\qquad} \underline{\qquad} \underline{\qquad} \underline{\qquad}$	\xrightarrow{K} J
Corollary to the Base Angles Theorem	Λ
If a triangle is, then it is	\mathcal{A}
×	$\boldsymbol{\lambda}$
Corollary to the Converse of Base Angles Theorem	
If a triangle is, then it is	
	•
Find ST	ст
Find m∠T	3 5

Find the values of x and y



Assignment: 248 #2, 4, 6, 8, 12, 14, 16, 18, 20, 21, 22, 24, 27, 28, 30, 36, 38, 39, 40, 43 = 20 total

5.5 Proving Triangles Congruent by SSS

SSS (Side-Side	e-Side Congruence Pos	tulate)			
If	_ of one triangle are	to	of anoth	er triangle, then the _	are
True or False			F	J	
$\Delta DFG \cong \Delta HJK$ $\Delta ACB \cong \Delta CAD$				H K	$A \xrightarrow{3} \xrightarrow{B} \xrightarrow{7} C$
Given: $\overline{AB} \cong \overline{DC}$	$\overline{C}; \overline{AD} \cong \overline{BC}$				
Prove: $\triangle ABD \cong$	ΔCDB	1		A	В
Statements		Reasons			
1.		1.		T.	
2.		2.		D	C
3.		3.			
Determine whe	ther the figure is stable.				

HL

Right triangles are special

If we know two sides are congruent we can use the Pythagorean Theorem (ch 7) to show that the third sides are congruent





Assignment: 256 #1, 2, 3, 4, 6, 7, 8, 10, 12, 14, 18, 20, 22, 26, 28, 31, 32, 34, 35, 36 = 20 total

Geometry 5.6

Geometry

5.6 Proving Triangles Congruent by ASA and AAS



Given: $\overline{DH} \parallel \overline{GF}, \overline{DH} \cong \overline{GF}$ Prove: $\triangle DEH \cong \triangle GEF$ StatementsReasons1.1.2.2.3.3.





Given: $\overline{RS} \cong \overline{VU}, \angle S \cong \angle U$ Prove: $\triangle RST \cong \triangle VUT$

110 Ve. $\Delta N S I = \Delta V S I$		
Statements	Reasons	
1.	1.	$+$ \times
2.	2.	s
3.	3.	

Assignment: 264 #2, 4, 6, 8, 12, 14, 16, 22, 24, 28, 35, 38, 39, 40, 41 = 15 total

5.7 Using Congruent Triangles



Assignment: 271 #2, 3, 4, 6, 8, 10, 13, 17, 19, 20, 23, 25, 26, 27, 28 = 15 total

5.8 Coordinate Proofs

Coordi	nate Proof				
Place g	eometric	in a	plane ()	
When_		are used for	r the	, the result is true for	figures of that type
Use for	mulas to prove	things			
•		formula			
			$Midpt = \left(\frac{x_1 + x_2}{2}\right)$	$\left(\frac{x_2}{2}, \frac{y_1 + y_2}{2}\right)$	
•		formula			
			$d = \sqrt{(x_2 - x_1)}$	$(x^2 + (y_2 - y_1))^2)$	
•		formula			
			$m = \frac{y_2}{x_2}$	$\frac{-y_1}{-x_1}$	
1.	Use the	as a	or		
2.	Place at least o	one	of the polygon on an	_	
3.	Usually keep t	the v	within the		
4.	Use	that ma	akeas	as possible.	
•	You will prove	e things by	things like	,, and	
	←	(0, k) k (0, 0)	(h, k)	*	(0, 0) (<i>f</i> , <i>g</i>) (<i>d</i> , 0) <i>x</i>
Place a	square in a coo	ordinate plane	so that it is convenient for fir	ding side lengths. Assign	coordinates.
Place a	right triangle	in a coordinate	e plane so that it is convenien	t for finding side lengths. A	Assign coordinates.

Place an isosceles triangle in a coordinate plane with vertices P(-2a, 0), Q(0, a), and R(2a, 0). Then find the side lengths and the coordinates of the midpoint of each side.

Given: Coordinates of vertices of quadrilateral *OTUV* Prove: $\angle TOU \cong \angle VUO$



Assignment: 277 #2, 4, 6, 8, 11, 12, 15, 16, 22, 23, 25, 26, 29, 32, 33 = 15 total



	Write a proof.		^B	
	GIVEN $\blacktriangleright \triangle ABC$ is isosceles with base \overline{AC} , \overline{BD} bisects $\angle B$.	\angle		\leq
21.	PROVE $\blacktriangleright \triangle ABD \cong \triangle CBD$	А	D	С

Answers		
1.	ΔΑΒΕ	$\overline{AB} \cong \overline{BC}$ (Definition of isosceles tri-
2.	ΔBCD	angle)
3.	ΔBDE	$\angle ABD \cong \angle CBD$ (Definition of angle bi-
4.	ΔBDE	sector)
5.	ΔBCD	$\overline{BD} \cong \overline{BD}$ (Reflexive)
6.	ΔΑΒΕ	$\Delta ABD \cong \Delta CBD$ (SAS)
7.	ASA	
8.	HL	
9.	SSS	
10.	AAS	
11.	SAS	
12.	Not Possible	
13.	134	
14.	36	
15.	18	
16.	30	
17.	25	
18.	6	
19.	(0, a) (a, a) (a, a) (a, a) (a, 0) (a, 0) (a, 0) (a, 0) (a, 0) (a, 0) (b, 0)	
20.	I	
21.	$\triangle ABC$ is isosceles, \overline{BD} bisects $\angle B$	
	(Given)	